



## Numerical study on influence of a type of nanoparticles and volume fraction on turbulent heat transfer coefficient and pressure loss inside a tube

R. Davarnejad\*, M. Hekmat

Chemical Engineering Department, Faculty of Engineering, Arak University, Arak, Iran

**ABSTRACT:** Conventional liquids have some limitations regarding the thermal properties. The nanoparticles addition is one of the techniques which can transcend them. In this research, heat transfer coefficient ( $h$ ) and pressure loss ( $\Delta p$ ) of various nanofluids containing  $Al_2O_3$ ,  $SiO_2$ , and  $MgO$  nanoparticles dispersed in water in an annular tube with constant wall temperature is considered. According to the literature, five different nanofluid volume concentrations (1%, 2%, 3%, 4% and 5%) are selected. Two models involving the mixture and VOF are applied, and the results are compared. The average convective heat transfer coefficient and pressure loss is enhanced with volume fraction and Reynolds number ( $Re$ ) increment ( $3000 < Re < 10000$ ) although the friction factor ( $f$ ) is decreased. It is concluded that the simulated data for pressure loss and heat transfer coefficient were in good agreement with the experimental ones specially for  $SiO_2$  nanoparticles (particularly in low concentrations). The  $SiO_2$  nanofluid showed the best heat transfer compared to the other nanofluids. Moreover, the simulated data obtained from the mixture method showed more agreement with the experimental ones specially the high Reynolds numbers.

### Review History:

Received: 22 August 2017  
Revised: 31 October 2017  
Accepted: 20 February 2018  
Available Online: 1 March 2018

### Keywords:

Fluent  
Nanofluid  
Turbulent  
Volume fraction

### 1- Introduction

A nanofluid is a fluid containing suspended solid particles with nanometer dimensions (1–100 nm) [1]. Nanofluids can be considered as a new class of solid-liquid composite materials consisting of solid nanoparticles. Typical nanoparticles in water-based nanofluids are metals and oxides such as  $Al_2O_3$ ,  $SiO_2$ ,  $MgO$ , etc. Normally, nanofluids have higher thermal conductivity than their base fluids [2-5].

According to a research done by Ting and Hou, the heat transfer is increased with increasing particles concentration and Peclet number [6]. In another research, the heat transfer is increased with adding nanoparticles in a fluid [7]. Furthermore, heat transfer coefficient is increased with increasing the nanoparticle concentration in a nanofluid. The natural convection of water-based nanofluid in a square cavity was numerically studied in the literature [8]. In the recent paper, the nanofluid-oriented model for calculation of the effective thermal conductivity and another model for the effective dynamic viscosity calculation were applied.

The friction factor and forced convection heat transfer of  $TiO_2$  nanoparticles dispersed in water of a car's radiator were numerically determined. The Reynolds number (from 10000 to 100000) and inlet temperature (from 60 to 90 °C) were studied in this research. The results showed that the friction factor is decreased with increasing the Reynolds number and concentration. The  $TiO_2$  nanoparticles at low concentrations can increase the heat transfer efficiency up to 20% compared with the pure water [9]. According to a research done by Davarnejad and Jamshidzadeh, the Nusselt number is increased with increasing the volume fraction of nanofluid [10].

Corresponding author, E-mail: R-Davarnejad@araku.ac.ir

In another research, the thermal conductivity, viscosity and turbulent heat transfer behavior of Magnesium Oxide-water nanofluid in a circular pipe (when volume fraction of nanoparticle in the base fluid was less than 1%) were experimentally investigated [11]. The most of the conventional models were unable to predict the thermal conductivity and dynamic viscosity of  $MgO$ -water nanofluid.

In the current research, a new correlation for the dynamic viscosity prediction was applied. The simulation was carried out in a fully developed turbulent regime. The conditions were exactly extracted from the experimental work [12]. The simulated data (obtained from two models: mixture and VOF model) were compared with each other and the experimental ones.

### 2- Simulation

A heat exchanger applied in the literature [12, 13] was simulated by Fluent software (version: 6.3.26). It was an annular tube with constant wall temperature (78 °C). Its length and diameter of tube were 1.5 m and 0.64 cm, respectively. The initial temperature of nanofluid was 25 °C.

Gambit was applied under the Fluent software [14]. The tube was meshed with an interval count option. The mesh number in the vertical and horizontal directions were respectively found at 0.001067 and 0.03 according to the tube dimensions and interval count amount.

In Computational Fluid Dynamics (CFD), the Volume of Fluid (VOF) method is a numerical technique for tracking and locating the free surface (or fluid-fluid interface). In fact, it is a numerical recipe which allows the programmer to track the shape and position of interfaces. The Navier-Stokes equations are also solved to analyze the flow motion [15].

A nanofluid contains small particles without phase separation

**Table 1. Nanoparticles properties**

Nanoparticle	Density (kg/m <sup>3</sup> )	Specific heat capacity (J/ kg. K)	Molecular weight (kg/ kmole)	Conductivity [kg/(m. s)]
Al <sub>2</sub> O <sub>3</sub>	4100	880	101.963	35
MgO	3580	960	40.312	45
SiO <sub>2</sub>	2200	733	60	1.38

**Table 2. Friction factor compared with the base fluid (Re = 3000-10000)**

Nanoparticle type	Nanoparticle volume fraction percentage				
	0.005	0.01	0.02	0.03	0.04
Al <sub>2</sub> O <sub>3</sub> (experiment)	-1%	-0.2%-0.9%	-1.6%-(-0.9%)	-1.9%-0.1%	-1%
Al <sub>2</sub> O <sub>3</sub> (mixture)	-0.003%	-0.11%	-0.15%	-0.18%	-0.25%
Al <sub>2</sub> O <sub>3</sub> (VOF)	≅0	-0.07%	-0.12%	-0.15%	-0.25%
MgO (experiment)	0.2%-7%	1%-2.9%	-0.1%-5.2%		
MgO (mixture)	-0.032%	-0.11%	-0.16%		
MgO (VOF)	≅0	-0.07%	-0.12%		
SiO <sub>2</sub> (experiment)	(-4.6%)-(+0.6%)	(-4.9%)-(-2%)	-8.1%-(-1.1%)	(-8.2%)-(-0.6)%	-2.2%-7.6%
SiO <sub>2</sub> (mixture)	-2.2%	-4.58%	-10.54%	-12.31%	-16.32%
SiO <sub>2</sub> (VOF)	0.02%	-3.69%	-7.78%	-10.3%	-14.79%

and sedimentation. It also shows a dramatic new property [16]. Table 1 shows nanoparticles data. The particles were assumed to be in a spherical shape. Therefore,  $\psi$  and  $n$  are 3 and 1, respectively [17]. The nanofluids characteristics can be obtained from the following equations [18,19]:

$$c_{p,nf} = \frac{\phi c_{p,p} P_p + (1-\phi) P_{bf} c_{p,nf}}{P_{nf}} \quad (1)$$

$$\rho_{nf} = \phi \rho_p + (1-\phi) \rho_f \quad (2)$$

$$\frac{k_{nf}}{k_f} = \frac{k_p + (n-1)k_f + (n-1)\phi(k_p - k_f)}{k_p + (n-1)k_f - \phi(k_p - k_f)} \quad (3)$$

Furthermore, a model which predicts the nanofluid viscosity is presented as [20]:

$$\mu_{nf;wang} = (1 + 7.3\phi + 123\phi^2) \mu_f \quad (4)$$

where,  $\mu$  and  $\mu_f$  are nanofluid and water viscosity, respectively.

The friction factor ( $f$ ) is determined by [21]:

$$f = 2\Delta p d / \rho v^2 l \quad (5)$$

where  $\Delta p$  denotes the pressure loss.

### 3- Results and Discussion

The convective heat transfer and pressure losses grow by adding nanoparticles to the base fluid. According to the literature, pressure loss is increased with Reynolds number and volume fraction increment [13].

Table 2 shows friction factor ( $f$ ) for nanofluids and base fluid (water) in the turbulent region. The friction factor is increased with increasing the pressure loss and nanoparticles volume fraction in the pipe [12, 22]. As shown in equation (5), there

is a direct relation between the friction factor and the pressure loss. A sharper difference was also observed between SiO<sub>2</sub> nanofluid and the base fluid. Its reason may be due to having smaller size of SiO<sub>2</sub> nanoparticles compared with the other ones.

Fig. 1 shows the enhancement of simulated data for pressure loss at various nanoparticles concentration versus Reynolds number. As shown in Fig. 1, simulated data (for pressure loss) are in good agreement with the experimental ones in specially for SiO<sub>2</sub> (Maximum error is 18% and minimum error is 1.02%). Furthermore, the simulated data obtained from the mixture method is in more agreement with the experimental ones in the higher Reynolds numbers. It also needs a shorter convergence time. Its reason may be due to having more homogenous solution in the high Reynolds numbers [13, 21]. The heat transfer coefficient of all nanofluids is significantly higher than that of the base fluid. The experimental results illustrate that addition of flow value of nanoparticles to pure water (around 0.0625%) improved the heat transfer performance significantly [13].

Fig. 2 shows simulated data for turbulent heat transfer coefficient of nanofluid for various nanoparticles concentration versus Reynolds number. As shown in Fig. 2, the simulated data for heat transfer coefficient is increased with increasing the Reynolds number and the nanoparticle concentration.

The simulated data for turbulent heat transfer coefficient are in good agreement with the experimental ones specially for SiO<sub>2</sub> (the maximum error is 14% and minimum error is 3.8%). The simulated data more agree with the experimental ones in low velocities.

The MgO-water nanofluids at five different volumetric concentrations (1%, 0.5%, 0.25%, 0.125% and 0.0625%) were examined. The Reynolds number varied from 3200 to

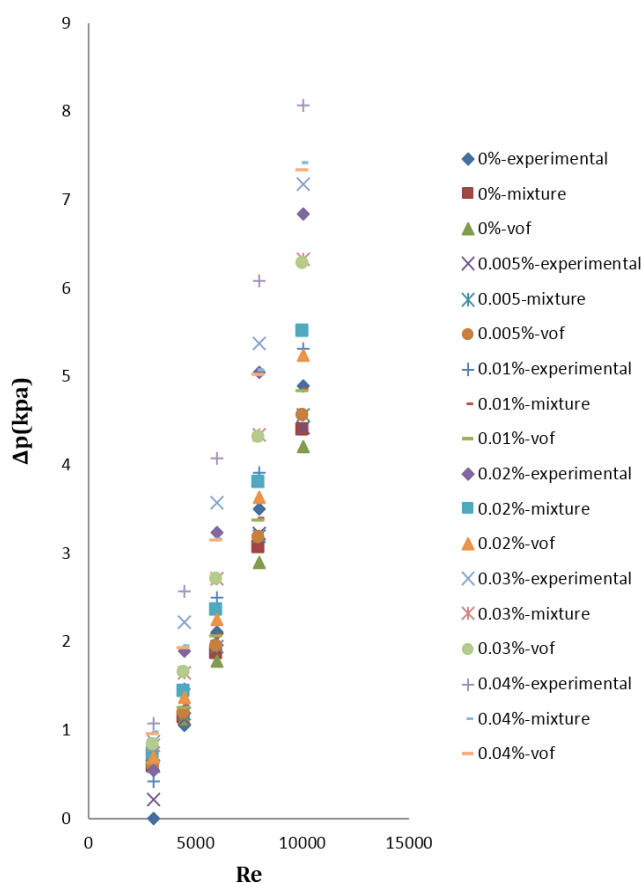


Fig 1. Pressure loss of SiO<sub>2</sub> nanofluids versus Reynolds number

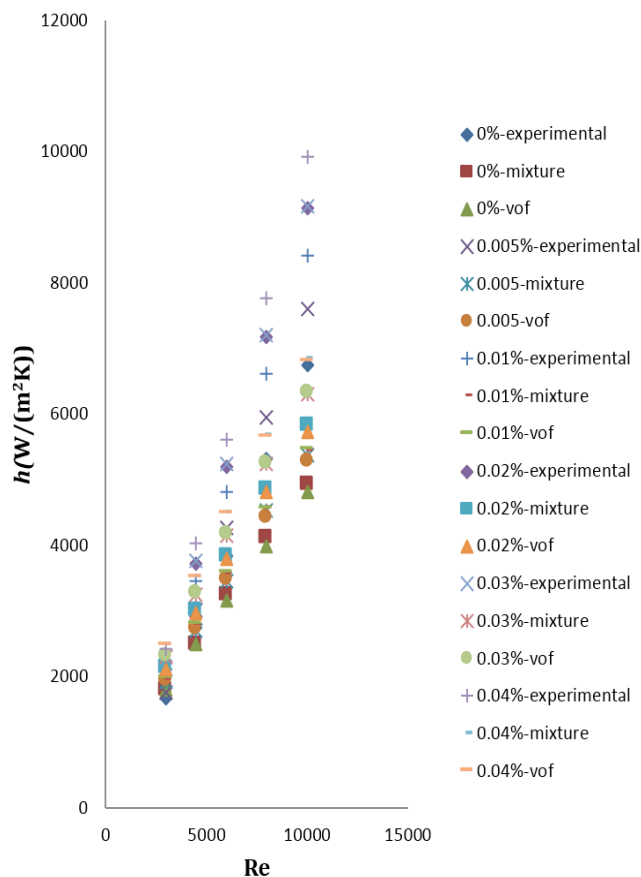


Fig 2. Turbulent heat transfer coefficient of SiO<sub>2</sub> nanofluids versus Reynolds number

19000. It was observed that the heat transfer coefficient of all nanofluids is significantly higher than that of the base fluid. The experimental results illustrate that adding low value of nanoparticles to pure water improves the heat transfer performance significantly [11].

Table 3 shows nanofluid turbulent heat transfer coefficient compared with the base fluid (3000 < Re < 10000). It was obtained that the heat transfer coefficient increases for all of nanofluids (compared with the base fluid) by the volume fraction increment [12]. According to a research carried out with applying a two-phase mixture model, finite volume method, and second-order upstream difference scheme, the convective heat transfer coefficient increases and the surface friction coefficient of an inclined tube decreases with increasing the Reynolds number. Furthermore, the convection heat transfer coefficient increases with increasing the volume fraction of nanoparticles [23]. According to another simulation work on Al<sub>2</sub>O<sub>3</sub>, TiO<sub>2</sub> and SiO<sub>2</sub> nanofluids, the friction factor and Nusselt number increases with increasing the volume concentration [24].

#### 4- Conclusions

It was concluded that the convective heat transfer coefficient increases with the nanoparticle volume fraction increment up to 4% in the turbulent regime. The applied Reynolds number varies in the interval [3000 10000]. The data were obtained from the two models (involving VOF and mixture) and compared. According to the experimental work [10] and out simulation, the heat transfer coefficient and the pressure loss increases with increasing volume fraction of nanofluids, although friction factor (*f*) was decreased. The simulated

data for pressure loss and heat transfer coefficient are in good agreement with the experimental ones specially for nano-SiO<sub>2</sub> (particularly in low concentrations). Furthermore, the SiO<sub>2</sub> nanoparticles showed the best heat transfer. The simulated data obtained from the mixture method showed more agreement with the experimental ones [13] specially in high Reynolds numbers.

#### Nomenclature

- $C_p$  specific heat, J/kg K
- $\mu$  viscosity, pa.s
- $\rho$  density, kg/m<sup>3</sup>
- $f$  friction factor
- $\varphi$  nanoparticles volume fraction
- $\Delta p$  pressure drop, kpa
- $\psi$  particle sphericity
- $d$  tube diameter, m
- $K$  thermal conductivity, W/m
- $K_n$  empirical shape factor
- $v$  mean velocity, m/s
- $l$  tube length, m

#### Subscripts

- bf** base fluid
- nf** nanofluid
- p** particle

**Table 3. Nanofluid turbulent heat transfer coefficient compared with the base fluid (Re = 3000-10000)**

Nanoparticle type	Nanoparticle volume fraction percentage				
	0.005	0.01	0.02	0.03	0.04
Al <sub>2</sub> O <sub>3</sub> (experiment)	10.50%	6.6%-28.4%	15.3%-32.5%	33.5%-40.2%	46.3%
Al <sub>2</sub> O <sub>3</sub> (mixture)	12.55%	21.83%	34.11%	44.9%	53.76%
Al <sub>2</sub> O <sub>3</sub> (VOF)	11.77%	32.08%	33.38%	43.15%	49.73%
MgO (experiment)	(-2.8%)-(+9.9%)	6.3%-24.6%			
MgO (mixture)	16.53%	24.81%			
MgO (VOF)	15.64%	24.19%			
SiO <sub>2</sub> (experiment)	10.4%-15.5%	23.2%-28.2%	23%-32.6%	23.7%-35.1%	26.4%-46.7%
SiO <sub>2</sub> (mixture)	8.03%	10.73%	18.65%	27.94%	39.26%
SiO <sub>2</sub> (VOF)	9.90%	13.54%	19.20%	31.11%	41.32%

**References**

[1] P. Bhattacharya, S.K. Saha, A. Yadav, P.E. Phelan, R.S. Prasher, Brownian dynamics simulation to determine the effective thermal conductivity of nanofluids, *Journal of Applied Physics*, 95(11) (2004) 6492-6494.

[2] T.T. Baby, S. Ramaprabhu, Enhanced convective heat transfer using graphene dispersed nanofluids, *Nanoscale Research Letters*, 6(1) (2011) 289.

[3] S.K. Das, S.U. Choi, W. Yu, T. Pradeep, *Nanofluids: science and technology*, John Wiley & Sons, 2007.

[4] H. Xie, J. Wang, T. Xi, Y. Liu, F. Ai, Dependence of the thermal conductivity of nanoparticle-fluid mixture on the base fluid, *Journal of Materials Science Letters*, 21(19) (2002) 1469-1471.

[5] J. Buongiorno, D.C. Venerus, N. Prabhat, T. McKrell, J. Townsend, R. Christianson, Y.V. Tolmachev, P. Keblinski, L.-w. Hu, J.L. Alvarado, I.C. Bang, S.W. Bishnoi, M. Bonetti, F. Botz, A. Cecere, Y. Chang, G. Chen, H. Chen, S.J. Chung, M.K. Chyu, S.K. Das, R. Di Paola, Y. Ding, F. Dubois, G. Dzido, J. Eapen, W. Escher, D. Funfschilling, Q. Galand, J. Gao, P.E. Gharagozloo, K.E. Goodson, J.G. Gutierrez, H. Hong, M. Horton, K.S. Hwang, C.S. Iorio, S.P. Jang, A.B. Jarzebski, Y. Jiang, L. Jin, S. Kabelac, A. Kamath, M.A. Kedzierski, L.G. Kieng, C. Kim, J.-H. Kim, S. Kim, S.H. Lee, K.C. Leong, I. Manna, B. Michel, R. Ni, H.E. Patel, J. Philip, D. Poulidakos, C. Reynaud, R. Savino, P.K. Singh, P. Song, T. Sundararajan, E. Timofeeva, T. Triticak, A.N. Turanov, S. Van Vaerenbergh, D. Wen, S. Witharana, C. Yang, W.-H. Yeh, X.-Z. Zhao, S.-Q. Zhou, A benchmark study on the thermal conductivity of nanofluids, *Journal of Applied Physics*, 106(9) (2009) 094312.

[6] H.-H. Ting, S.-S. Hou, Numerical study of laminar flow and convective heat transfer utilizing nanofluids in equilateral triangular ducts with constant heat flux, *Materials*, 9(7) (2016) 576.

[7] S. Zeinali Heris, M. Nasr Esfahany, S.G. Etemad, Experimental investigation of convective heat transfer of Al<sub>2</sub>O<sub>3</sub>/water nanofluid in circular tube, *International Journal of Heat and Fluid Flow*, 28(2) (2007) 203-210.

[8] G.C. Nikiforidis, E.D. Skouras, G.C. Bourantas, V.C. Loukopoulos, Natural convection of nanofluids flow with “nanofluid-oriented” models of thermal conductivity and dynamic viscosity in the presence of heat source, *International Journal of Numerical Methods for Heat & Fluid Flow*, 23(2) (2013) 248-274.

[9] A.M. Hussein, H.K. Dawood, R.A. Bakara, K. Kadrigamaa, Numerical study on turbulent forced convective heat transfer using nanofluids TiO<sub>2</sub> in an automotive cooling system, *Case Studies in Thermal Engineering*, 9 (2017) 72-78.

[10] R. Davarnejad, M. Jamshidzadeh, CFD modeling of heat transfer performance of MgO-water nanofluid under turbulent flow, *Engineering Science and Technology, an International Journal*, 18(4) (2015) 536-542.

[11] M. Hemmat Esfe, S. Saedodin, M. Mahmoodi, Experimental studies on the convective heat transfer performance and thermophysical properties of MgO-water nanofluid under turbulent flow, *Experimental Thermal and Fluid Science*, 52 (2014) 68-78.

[12] S. Zeinali Heris, S.G. Etemad, M. Nasr Esfahany, Experimental investigation of oxide nanofluids laminar flow convective heat transfer, *International Communications in Heat and Mass Transfer*, 33(4) (2006) 529-535.

[13] A. Meriläinen, A. Seppälä, K. Saari, J. Seitsonen, J. Ruokolainen, S. Puisto, N. Rostedt, T. Ala-Nissila, Influence of particle size and shape on turbulent heat transfer characteristics and pressure losses in water-based nanofluids, *International Journal of Heat and Mass Transfer*, 61 (2013) 439-448.

[14] R. Davarnejad, S. Barati, M. Zakeri, Simulation of convective heat transfer of a nanofluid in a circular crosssection, *International Journal of Engineering-Transactions C: Aspects*, 26(6) (2012) 571.

[15] H.K. Versteeg, W. Malalasekera, *An introduction to computational fluid dynamics: the finite volume method*, Pearson education, 2007.

[16] S.U.S. Choi, J.A. Eastman, *Enhancing thermal conductivity of fluids with nanoparticles*, Argonne National Lab., IL (United States), 1995.

[17] R.L. Hamilton, O.K. Crosser, *Thermal Conductivity of Heterogeneous Two-Component Systems*, Industrial &

- Engineering Chemistry Fundamentals, 1(3) (1962) 187-191.
- [18] B.C. Pak, Y.I. Cho, Hydrodynamic and heat transfer study of dispersed fluids with submicron metallic oxide particles, *Experimental Heat Transfer an International Journal*, 11(2) (1998) 151-170.
- [19] Y. Xuan, W. Roetzel, Conceptions for heat transfer correlation of nanofluids, *International Journal of Heat and Mass Transfer*, 43(19) (2000) 3701-3707.
- [20] X. Wang, X. Xu, S.U. S. Choi, Thermal conductivity of nanoparticle-fluid mixture, *Journal of thermophysics and heat transfer*, 13(4) (1999) 474-480.
- [21] F.P. Incropera, A.S. Lavine, T.L. Bergman, D.P. DeWitt, *Fundamentals of heat and mass transfer*, Wiley, 2007.
- [22] K.B. Anoop, T. Sundararajan, S.K. Das, Effect of particle size on the convective heat transfer in nanofluid in the developing region, *International Journal of Heat and Mass Transfer*, 52(9) (2009) 2189-2195.
- [23] F. Vahidinia, M. Miri, Numerical study of the effect of the Reynolds numbers on thermal and hydrodynamic parameters of turbulent flow mixed convection heat transfer in an inclined tube/Numericna raziskava vpliva Reynoldsovega stevila na toplotne in hidrodinamicne parametre mesanega konvektivnega prenosa toplote s turbulentnim tokom v posevni cevi, *Strojniski Vestnik-Journal of Mechanical Engineering*, 61(11) (2015) 669-681.
- [24] A.M. Hussein, K.V. Sharma, R.A. Bakar, K. Kadirgama, The effect of nanofluid volume concentration on heat transfer and friction factor inside a horizontal tube, *Journal of Nanomaterials*, 2013 (2013) 1.

Please cite this article using:

R. Davarnejad and M. Hekmat, Numerical study on influence of a type of nanoparticles and volume fraction on turbulent heat transfer coefficient and pressure loss inside a tube, *AUT J. Model. Simul.*, 50(2) (2018) 123-128.

DOI: 10.22060/miscj.2018.13315.5069



